

---

Addendum to  
NIST Special Publication 800-38A  
October, 2010

**NIST**

**National Institute of  
Standards and Technology**

U.S. Department of Commerce

**Recommendation for Block  
Cipher Modes of Operation:  
Three Variants of Ciphertext  
Stealing for CBC Mode**

Morris Dworkin

---

C O M P U T E R   S E C U R I T Y

---



Addendum to  
NIST Special Publication 800-38A

# **Recommendation for Block Cipher Modes of Operation: Three Variants of Ciphertext Stealing for CBC Mode**

Morris Dworkin

## ***C O M P U T E R   S E C U R I T Y***

Computer Security Division  
Information Technology Laboratory  
National Institute of Standards and Technology  
Gaithersburg, MD 20899-8930

October 2010



*U.S. Department of Commerce*  
*Gary Locke, Secretary*

*National Institute of Standards and Technology*  
*Patrick Gallagher, Director*

*Reports on Information Security Technology*

The Information Technology Laboratory (ITL) at the National Institute of Standards and Technology (NIST) promotes the U.S. economy and public welfare by providing technical leadership for the Nation's measurement and standards infrastructure. ITL develops tests, test methods, reference data, proof of concept implementations, and technical analyses to advance the development and productive use of information technology. ITL's responsibilities include the development of technical, physical, administrative, and management standards and guidelines for the cost-effective security and privacy of sensitive unclassified information in Federal computer systems. This Special Publication 800-series reports on ITL's research, guidance, and outreach efforts in computer security, and its collaborative activities with industry, government, and academic organizations.

Certain commercial entities, equipment, or materials may be identified in this document in order to describe an experimental procedure or concept adequately. Such identification is not intended to imply recommendation or endorsement by the National Institute of Standards and Technology, nor is it intended to imply that the entities, materials, or equipment are necessarily the best available for the purpose.

**Addendum**  
**National Institute of Standards and Technology Special Publication 800-38A**  
**11 pages (June 2010)**  
**CODEN: NSPUE2**

Table of Contents

<b>1</b>	<b>INTRODUCTION</b> .....	<b>1</b>
<b>2</b>	<b>SPECIFICATION OF CBC-CS1</b> .....	<b>2</b>
<b>3</b>	<b>SPECIFICATION OF CBC-CS2</b> .....	<b>4</b>
<b>4</b>	<b>SPECIFICATION OF CBC-CS3</b> .....	<b>6</b>
	<b>REFERENCES</b> .....	<b>7</b>

List of Figures

Figure 1: CBC-CS1-Encrypt.....	3
Figure 2: CBC-CS1-Decrypt .....	4



## 1 Introduction

A limitation to Cipher Block Chaining (CBC) mode, as specified in NIST SP 800-38A, Ref. [1], is that the plaintext input must consist of a sequence of blocks. (In the rest of this publication, a block is called a “complete block” to emphasize the contrast with a “partial block” whose bit length is smaller than the block size.) Although Appendix A of Ref. [1] describes how padding methods can be used to meet this requirement, in such cases, the length of the resulting ciphertext expands over the length of the unpadded plaintext by the number of padding bits.

This addendum to Ref. [1] specifies three variants of CBC mode that accept any plaintext input whose bit length is greater than or equal to the block size, whether or not the length is a multiple of the block size. Unlike the padding methods discussed in Ref. [1], these variants avoid ciphertext expansion.

These variants are denoted CBC-CS1, CBC-CS2, and CBC-CS3, where “CS” indicates “ciphertext stealing,” because when padding bits are needed in these variants, they are taken from the penultimate ciphertext block. The variants differ only in the ordering of the ciphertext bits. CBC-CS1 was specified as a suggestion on the NIST Computer Security Resource Center web site. CBC-CS2 is specified, for example, in Ref. [3]. CBC-CS3 is the variant specified for Kerberos 5 in Ref. [2].

Below are the specifications for encryption and decryption using CBC-CS1, CBC-CS2, and CBC-CS3, building on the specification of the CBC encryption and decryption in Ref. [1]. Diagrams are given for CBC-CS1 encryption and decryption. Each variant inherits the relevant requirements of Ref. [1], e.g., on the underlying block cipher, the key, and the initialization vector.

The following notational conventions apply to the specifications below:

- Bit strings are denoted with upper case letters; integers with lower case letters.
- The block size of the underlying block cipher is denoted  $b$ .
- For a bit string  $X$ , the bit length of  $X$  is denoted  $\text{len}(X)$ .
- For a bit string  $X$  and a positive integer  $r$  that does not exceed  $\text{len}(X)$ , the string consisting of the leftmost  $r$  bits of  $X$  is denoted  $\text{MSB}_r(X)$ , and the string consisting of the rightmost  $r$  bits of  $X$  is denoted  $\text{LSB}_r(X)$ .
- For an input block  $B$  and key  $K$ , the output block of the cipher function (“encryption”) is denoted  $\text{CIPH}_K(B)$ , and the output block of the inverse cipher function (“decryption”) is denoted  $\text{CIPH}_K^{-1}(B)$ .

In principle, the input strings to encryption and decryption for each of the variants may be any string whose length is not less than  $b$  bits, but typically an implementation is designed to accept a restricted set of lengths. For example, the set of lengths may be

restricted to multiples of 8, so that the input strings may be represented with bytes/octets. The input lengths that an implementation allows are called the *valid* lengths.

## 2 Specification of CBC-CS1

### Algorithm: CBC-CS1-Encrypt

*Input:* plaintext  $P$ , such that  $\text{len}(P)$  is valid;  
 initialization vector  $IV$ ;  
 key  $K$ .

*Output:* ciphertext  $C$ , such that  $\text{len}(C)=\text{len}(P)$ .

*Steps:*

1. Let  $n$  be the smallest integer such that  $n \cdot b \geq \text{len}(P)$ , let  $d = \text{len}(P) - (n-1) \cdot b$ , and let  $P_1, P_2, \dots, P_{n-1}, P_n^*$  be the unique sequence of bit strings such that:
  - a)  $P = P_1 || P_2 || \dots || P_{n-1} || P_n^*$ ; and
  - b)  $P_1, P_2, \dots$  and  $P_{n-1}$  are complete blocks.
 Consequently,  $\text{len}(P_n^*) = d$ , and  $1 \leq d \leq b$ , so that  $P_n^*$  is either a complete block or a nonempty partial block.
2. Let  $PAD$  be the bit string consisting of  $b-d$  '0' bits, and let  $P_n = P_n^* || PAD$ . Note that if  $P_n^*$  is a complete block, then  $PAD$  is the empty string, and  $P_n = P_n^*$ .
3. Apply CBC encryption to the plaintext  $(P_1, P_2, \dots, P_{n-1}, P_n)$  with initialization vector  $IV$  and key  $K$  to produce  $(C_1, C_2, \dots, C_{n-1}, C_n)$ .
4. Let  $C_{n-1}^* = \text{MSB}_d(C_{n-1})$ .
5. Return  $C_1 || C_2 || \dots || C_{n-2} || C_{n-1}^* || C_n$ .

When  $P_n^*$  is a complete block, CBC-CS1-Encrypt is equivalent to CBC encryption.

*Diagram:* Figure 1 below illustrates the CBC-CS1-Encrypt algorithm for the case that  $P_n^*$  is a partial block, i.e.,  $d < b$ . The bolded rectangles contain the inputs and outputs. The dotted rectangles provide alternate representations of two blocks in order to illustrate the role of the "stolen" ciphertext.

In particular, the string of the  $b-d$  rightmost bits of  $C_{n-1}$ , denoted  $C_{n-1}^{**}$ , becomes the padding for the input block to the final invocation of the block cipher within the execution of CBC mode. The ciphertext that is returned in Step 5 above omits  $C_{n-1}^{**}$ , because it can be recovered from  $C_n$  during decryption.



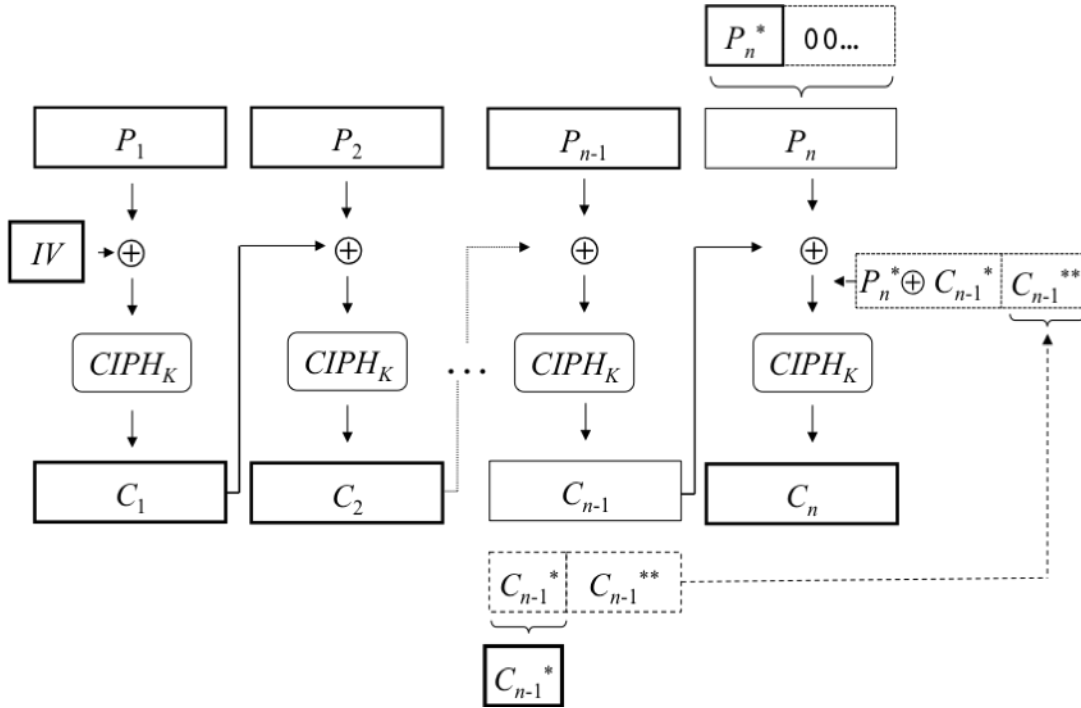


Figure 1: CBC-CS1-Encrypt

Algorithm: CBC-CS1-Decrypt

*Input:* ciphertext  $C$ , such that  $\text{len}(C)$  is valid;  
 initialization vector  $IV$ ;  
 key  $K$ .

*Output:* plaintext  $P$ , such that  $\text{len}(P) = \text{len}(C)$ .

*Steps:*

1. Let  $n$  be the smallest integer such that  $n \cdot b \geq \text{len}(C)$ , let  $d = \text{len}(C) - (n-1) \cdot b$ , and let  $C_1, C_2, \dots, C_{n-2}, C_{n-1}^*, C_n$  be the unique sequence of bit strings such that
  - a)  $C = C_1 || C_2 || \dots || C_{n-2} || C_{n-1}^* || C_n$ ;
  - b)  $C_n$  is a complete block; and
  - c) if  $n > 2$ , then  $C_1, \dots, C_{n-2}$ , are complete blocks.

Consequently,  $\text{len}(C_{n-1}^*) = d$ , and  $1 \leq d \leq b$ , so that  $C_{n-1}^*$  is either a complete block or a nonempty partial block.

2. Let  $Z^* = \text{MSB}_d(\text{CIPH}_K^{-1}(C_n))$ , and  $Z^{**} = \text{LSB}_{b-d}(\text{CIPH}_K^{-1}(C_n))$ .
3. Let  $C_{n-1} = C_{n-1}^* || Z^{**}$ . Note that if  $C_{n-1}^*$  is a complete block, then  $Z^{**}$  is the empty string, and  $C_{n-1} = C_{n-1}^*$ .
4. Apply CBC decryption to  $(C_1, C_2, \dots, C_{n-1})$  with initialization vector  $IV$  and key  $K$  to produce  $(P_1, P_2, \dots, P_{n-1})$ .

5. Let  $P_n^* = C_{n-1}^* \oplus Z^*$ .
6. Return  $P_1 || P_2 || \dots || P_{n-1} || P_n^*$ .

When  $C_{n-1}^*$  is a complete block, CBC-CS1-Decrypt is equivalent to CBC decryption.

*Diagram:*

Figure 2 below illustrates the CBC-CS1-Decrypt algorithm for the case that  $C_{n-1}^*$  is a partial block, i.e.,  $d < b$ . As in the previous diagram, the bolded rectangles contain the inputs and outputs.

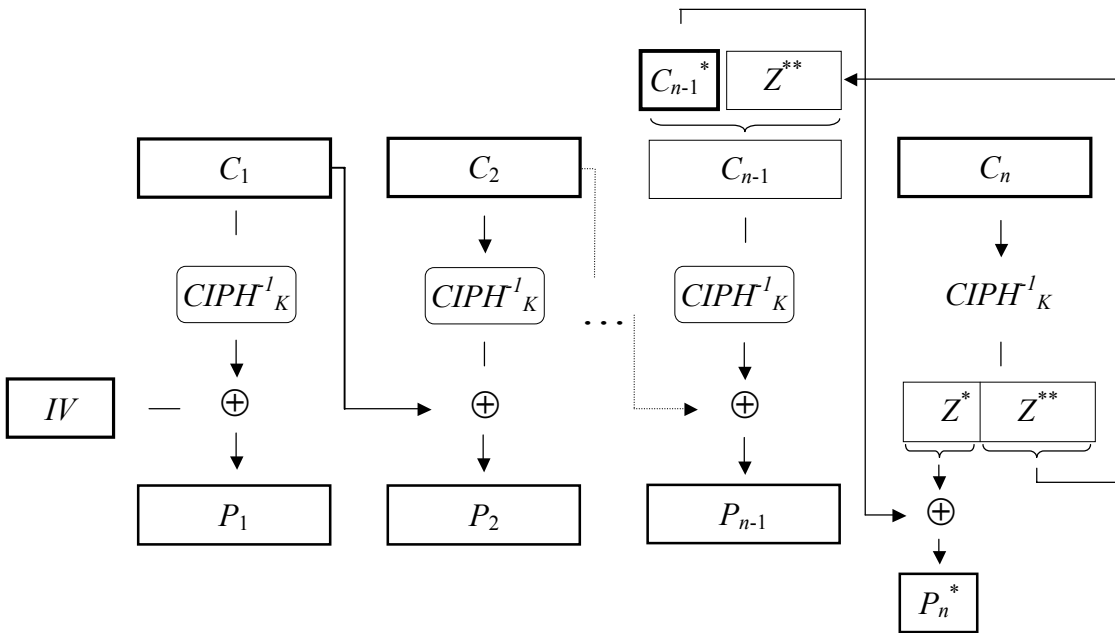


Figure 2: CBC-CS1-Decrypt

### 3 Specification of CBC-CS2

Algorithm: CBC-CS2-Encrypt

*Input:* plaintext  $P$ , such that  $\text{len}(P)$  is valid;  
 initialization vector  $IV$ ;  
 key  $K$ .

*Output:* ciphertext  $C$ , such that  $\text{len}(C) = \text{len}(P)$ .

*Steps:*

1. Let  $n$  be the smallest integer such that  $n \cdot b \geq \text{len}(P)$ , let  $d = \text{len}(P) - (n-1) \cdot b$ , and let  $P_1, P_2, \dots, P_{n-1}, P_n^*$  be the unique sequence of bit strings such that:
  - a)  $P = P_1 || P_2 || \dots || P_{n-1} || P_n^*$ ; and
  - b)  $P_1, P_2, \dots$  and  $P_{n-1}$  are complete blocks.
 Consequently,  $\text{len}(P_n^*) = d$ , and  $1 \leq d \leq b$ , so that  $P_n^*$  is either a complete block or a nonempty partial block.
2. Apply CBC-CS1-Encrypt to the plaintext  $P$  with initialization vector  $IV$  and key  $K$  to produce  $C_1 || C_2 || \dots || C_{n-2} || C_{n-1}^* || C_n$ .
3. If  $d = b$ , return  $C_1 || C_2 || \dots || C_{n-2} || C_{n-1}^* || C_n$ ; if  $d < b$ , return  $C_1 || C_2 || \dots || C_{n-2} || C_n || C_{n-1}^*$ .

When  $P_n^*$  is a complete block, then CBC-CS2-Encrypt, like CBC-CS1-Encrypt, is equivalent to CBC encryption. When  $P_n^*$  is a partial block, then CBC-CS2-Encrypt and CBC-CS1-Encrypt differ only in the ordering of  $C_{n-1}^*$  and  $C_n$ .

Algorithm: CBC-CS2-Decrypt

*Input:* ciphertext  $C$ , such that  $\text{len}(C)$  is valid;  
 initialization vector  $IV$ ;  
 key  $K$ .

*Output:* plaintext  $P$ , such that  $\text{len}(P) = \text{len}(C)$ .

*Steps:*

1. Let  $n$  be the smallest integer such that  $n \cdot b \geq \text{len}(C)$ , let  $d = \text{len}(C) - (n-1) \cdot b$ , and let  $C_1, C_2, \dots, C_{n-2}, C_{n-1}, C_n^*$  be the unique sequence of bit strings such that
  - a)  $C = C_1 || C_2 || \dots || C_{n-2} || C_{n-1} || C_n^*$ ;
  - b)  $C_{n-1}$  is a complete block; and
  - c) If  $n > 2$ , then  $C_1, \dots, C_{n-2}$ , are complete blocks.
 Consequently,  $\text{len}(C_n^*) = d$ , and  $1 \leq d \leq b$ , so that  $C_n^*$  is either a complete block or a nonempty partial block.
2. If  $d = b$ , i.e.,  $C_n^*$  is a complete block, then apply CBC-CS1-Decrypt to  $C$  with initialization vector  $IV$  and key  $K$ , and return the result,  $P$ . STOP.
3. If  $d < b$ , i.e.,  $C_n^*$  is a partial block, then let  $C' = C_1 || C_2 || \dots || C_{n-2} || C_n^* || C_{n-1}$ .
4. Apply CBC-CS1-Decrypt to  $C'$ , and return the result,  $P$ .

Note that in Step 3,  $C_n^*$  precedes  $C_{n-1}$  in order to undo the corresponding swap within the ciphertext in Step 3 of CBC-CS2-Encrypt.

## 4 Specification of CBC-CS3

### Algorithm: CBC-CS3-Encrypt

*Input:* plaintext  $P$ , such that  $\text{len}(P)$  is valid;  
 initialization vector  $IV$ ;  
 key  $K$ .

*Output:* ciphertext  $C$ , such that  $\text{len}(C)=\text{len}(P)$ .

*Steps:*

1. Apply CBC-CS1-Encrypt to the plaintext  $P$  with initialization vector  $IV$  and key  $K$  to produce  $C_1\|C_2\|\dots\|C_{n-2}\|C_{n-1}^*\|C_n$ .
2. Return  $C_1\|C_2\|\dots\|C_{n-2}\|C_n\|C_{n-1}^*$ .

Note that in Step 2,  $C_{n-1}^*$  and  $C_n$  are unconditionally swapped, i.e., even when  $C_{n-1}^*$  is a complete block; therefore, CBC-CS3 is not strictly an extension of CBC mode. In the other case, i.e., when  $C_{n-1}^*$  is a nonempty partial block, CBC-CS3-Encrypt is equivalent to CBC-CS2-Encrypt.

### Algorithm: CBC-CS3-Decrypt

*Input:* ciphertext  $C$ , such that  $\text{len}(C)$  is valid;  
 initialization vector  $IV$ ;  
 key  $K$ .

*Output:* plaintext  $P$ , such that  $\text{len}(P)=\text{len}(C)$ .

*Steps:*

1. Let  $n$  be the smallest integer such that  $n \cdot b \geq \text{len}(C)$ , let  $d = \text{len}(C) - (n-1) \cdot b$ , and let  $C_1, C_2, \dots, C_{n-2}, C_{n-1}, C_n^*$  be the unique sequence of bit strings such that
  - a)  $C = C_1\|C_2\|\dots\|C_{n-2}\|C_{n-1}\|C_n^*$ ;
  - b)  $C_{n-1}$  is a complete block; and
  - c) If  $n > 2$ , then  $C_1, \dots, C_{n-2}$ , are complete blocks.
 Consequently,  $\text{len}(C_n^*) = d$ , and  $1 \leq d \leq b$ , so that  $C_n^*$  is either a complete block or a nonempty partial block.
2. Apply the CBC-CS1-Decrypt algorithm with initialization vector  $IV$  and key  $K$  to  $C_1\|C_2\|\dots\|C_{n-2}\|C_n^*\|C_{n-1}$ , and return the result,  $P$ .

Note that in Step 2,  $C_n^*$  precedes  $C_{n-1}$  in order to undo the corresponding swap that was performed within Step 2 of CBC-CS3-Encrypt.

## References

- [1] Dworkin, M., *NIST Special Publication 800-38A, 2001 Edition: Recommendation for Block Cipher Modes of Operation, Methods and Techniques*, December 2001, Natl. Inst. Stand. Technol. [Web page], <http://www.csrc.nist.gov/publications/nistpubs/800-38a/sp800-38a.pdf>.
- [2] Raeburn, K., *Request for Comments 3962: Advanced Encryption Standard (AES) Encryption for Kerberos 5*, Internet Engineering Task Force, February 2005.
- [3] Schneier, B., *Applied Cryptography, Second Edition: protocols, algorithms, and source code in C*. New York: Wiley, 1996.